

Nuclear Revision P	ack	Name: Class: Date:	
Time:	358 minutes		
Marks:	320 marks		
Comments:			

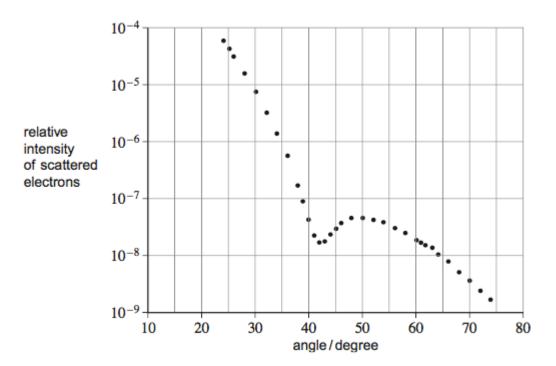
(a) The radius of a nucleus may be determined by electron diffraction. In an electron diffraction experiment a beam of electrons is fired at oxygen-16 nuclei. Each electron has an energy of  $5.94 \times 10^{-11}$  J.

1

The approximation, momentum =  $\frac{\text{energy}}{\text{speed of light}}$  can be used for electrons at this energy.

(i) Show that the de Broglie wavelength  $\lambda$  of each electron in the beam is about  $3.3 \times 10^{-15}$  m.

(ii) The graph shows how the relative intensity of the scattered electrons varies with angle due to diffraction by the oxygen-16 nuclei. The angle is measured from the original direction of the beam.



The angle  $\theta$  of the first minimum in the electron-diffraction pattern is given by

 $\sin \theta = \frac{0.61\lambda}{\text{nuclear radius}}$ 

Calculate the radius of an oxygen-16 nucleus using information from the graph.

radius = \_\_\_\_\_ m

(1)

(b) Rutherford used the scattering of  $\alpha$  particles to provide evidence for the structure of the atom.

(i) Sketch a labelled diagram showing the experimental arrangement of the apparatus used by Rutherford.

- (ii) State and explain the results of the scattering experiment. Your answer should include the following:
  - the main observations

2

- the significance of each observation
- how the observtions placed an upper limit on the nuclear radius.

The quality of your written communication will be assessed in your answer.

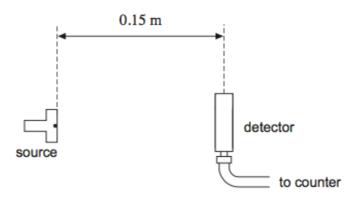
(6) (Total 11 marks)

(2)

 (a) The exposure of the general public to background radiation has changed substantially over the past 100 years.
 State and sources of radiation that has contributed to this change.

State **one** source of radiation that has contributed to this change.

(b) A student measures background radiation using a detector and determines that background radiation has a mean count-rate of 40 counts per minute. She then places a γ ray source 0.15 m from the detector as shown below.



With this separation the average count per minute was 2050.

The student then moves the detector further from the  $\gamma$  ray source and records the count-rate again.

(i) Calculate the average count-rate she would expect to record when the source is placed 0.90 m from the detector.

count-rate = \_\_\_\_\_ min<sup>-1</sup>

(3)

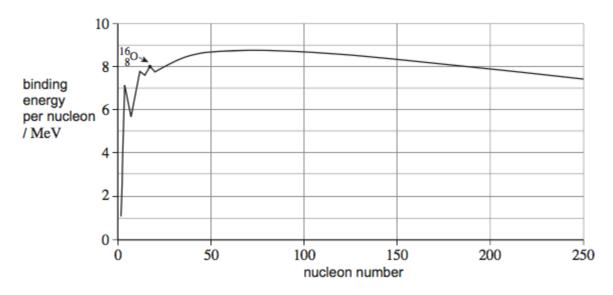
(ii) The average count per minute of 2050 was determined from a measurement over a period of 5 minutes. Explain why the student might choose to record for longer than 5 minutes when the separation is 0.90 m.

(1)

(iii)	When the detector was moved to 0.90 m the count-rate was lower than that calculated in part <b>(b)(i)</b> . It is suggested that the source may also emit $\beta$ partic	les.
	Explain how this can be checked.	
		_
		_
		_
		_
		_
		_
		_ (2)
		(Z) (Total 7 marks)

The diagram shows how the binding energy per nucleon varies with nucleon number.

3



(a)	(i)	Fission and fusion are two nuclear processes in which energy can be released. Explain why nuclei that undergo fission are restricted to a different part of the graph than those that undergo fusion.
	(ii)	Explain, with reference to the diagram, why the energy released per nucleon from fusion is greater than that from fission.
(b)	(i)	Calculate the mass difference, in kg, of the ${}^{16}_{8}$ O nucleus. mass of ${}^{16}_{8}$ O nucleus = 15.991 u

mass difference = \_\_\_\_\_ kg

(2)

(2)

(ii) Using your answer to part **(b)(i)**, calculate the binding energy, in MeV, of an oxygen <sup>16</sup><sub>8</sub>O nucleus.

binding energy = \_\_\_\_\_ MeV

(1)

- (iii) Explain how the binding energy of an oxygen  ${}^{16}_{8}$  O nucleus can be calculated with information obtained from the diagram.
- 4 An ancient sealed flask contains a liquid, assumed to be water. An archaeologist asks a scientist to determine the volume of liquid in the flask without opening the flask. The scientist decides to use a radioactive isotope of sodium (<sup>24</sup>Na) that decays with a half-life of 14.8 h.
  - (a) She first mixes a compound that contains  $3.0 \times 10^{-10}$  g of sodium-24 with 1500 cm<sup>3</sup> of water. She then injects 15 cm<sup>3</sup> of the solution into the flask through the seal. Show that initially about 7.5 × 10<sup>10</sup> atoms of sodium-24 are injected into the flask.

(1)

(b) Show that the initial activity of the solution that is injected into the flask is about  $1 \times 10^6$  Bq.

activity = \_\_\_\_\_Bq

(c) She waits for 3.5 h to allow the injected solution to mix thoroughly with the liquid in the flask. She then extracts 15 cm<sup>3</sup> of the liquid from the flask and measures its activity which is found to be 3600 Bq.

Calculate the total activity of the sodium-24 in the flask after 3.5 h and hence determine the volume of liquid in the flask.

(d) The archaeologist obtained an estimate of the volume knowing that similar empty flasks have an average mass of 1.5 kg and that mass of the flask and liquid was 5.2 kg. Compare the estimate that the archaeologist could obtain from these masses with the volume calculated in part 4.3 and account for any difference.

> (2) (Total 9 marks)

5

(a)

Which ionizing radiation produces the greatest number of ion pairs per mm in air? Tick ( $\checkmark$ ) the correct answer.

$\alpha$ particles	
$\beta$ particles	
γ rays	
X-rays	

(1)

(b) (i) Complete the table showing the typical maximum range in air for  $\alpha$  and  $\beta$  particles.

Type of radiation	Typical range in air / m
α	
β	

(2)

(ii)  $\gamma$  rays have a range of at least 1 km in air.

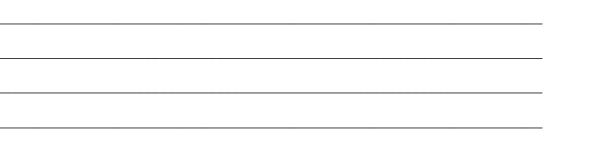
However, a  $\gamma$  ray detector placed 0.5 m from a  $\gamma$  ray source detects a noticeably smaller count-rate as it is moved a few centimetres further away from the source.

Explain this observation.

(1)

(c) Following an accident, a room is contaminated with dust containing americium which is an  $\alpha$ -emitter.

Explain the most hazardous aspect of the presence of this dust to an unprotected human entering the room.



(a) Scattering experiments are used to investigate the nuclei of gold atoms.
 In one experiment, alpha particles, all of the same energy (monoenergetic), are incident on a foil made from a single isotope of gold.

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(i) State the main interaction when an alpha particle is scattered by a gold nucleus.

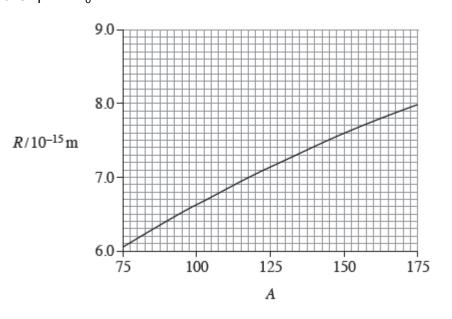
(ii) The gold foil is replaced with another foil of the same size made from a mixture of isotopes of gold. Nothing else in the experiment is changed.

Explain whether or not the scattering distribution of the monoenergetic alpha particles remains the same.

(1)

(b) Data from alpha-particle scattering experiments using elements other than gold allow scientists to relate the radius R, of a nucleus, to its nucleon number, A. The graph shows the relationship obtained from the data in a graphical form, which obeys

the relationship  $R = r_0 A^{\frac{1}{3}}$ 



(i) Use information from the graph to show that  $r_0$  is about  $1.4 \times 10^{-15}$  m.

(ii) Show that the radius of a  $\frac{51}{23}$  V nucleus is about 5 × 10<sup>-15</sup> m.

(2)

(1)

(c) Calculate the density of a  $\frac{51}{23}$ V nucleus.

7

State an appropriate unit for your answer.

density \_\_\_\_\_ unit \_\_\_\_\_

(3) (Total 8 marks)

A rod made from uranium-238 ( $^{238}_{92}$ U) is placed in the core of a nuclear reactor where it absorbs free neutrons.

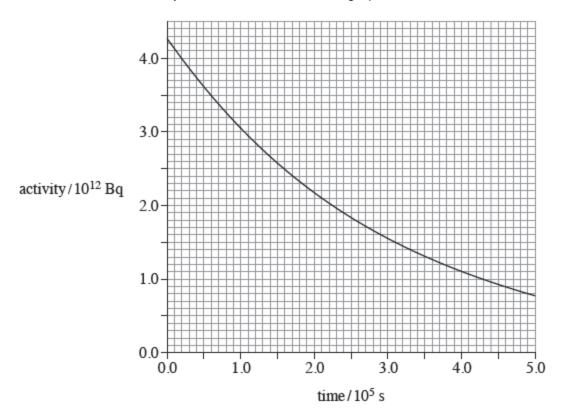
When a nucleus of uranium-238 absorbs a neutron it becomes unstable and decays to

neptunium–239 ( $^{239}_{\phantom{2}93}Np$ ), which in turn decays to plutonium–239 ( $^{293}_{\phantom{2}94}Pu$ ).

(a) Write down the nuclear equation that represents the decay of neptunium-239 into plutonium-239.

(b) A sample of the rod is removed from the core and its radiation is monitored from time t = 0 s.

The variation of the activity with time is shown in the graph.



(i) Show that the decay constant of the sample is about  $3.4 \times 10^{-6} \text{ s}^{-1}$ .

- (2)
- (ii) Assume that the activity shown in the graph comes only from the decay of neptunium. Estimate the number of neptunium nuclei present in the sample at time  $t = 5.0 \times 10^5$  s.

number of nuclei \_\_\_\_\_

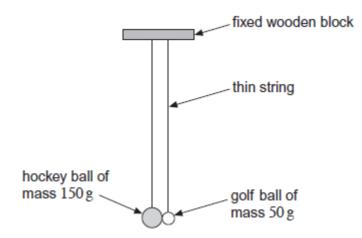
(1)

(c) (i) A chain reaction is maintained in the core of a thermal nuclear reactor that is operating normally.

Explain what is meant by a chain reaction, naming the materials and particles involved.

	(ii)	Explain the purpose of a moderator in a thermal nuclear reactor.	
			(2)
	(iii)		
		hazardous radiations. Radiation from the core includes $\alpha$ and $\beta$ particles, $\gamma$ ray X–rays, neutrons and neutrinos.	S,
		Explain why the shielding becomes radioactive.	
			(2)
		(Тс	otal 11 marks)
8	(a) Exp	plain what is meant by a <b>thermal</b> neutron.	
			(2)

(b) A student sets up the arrangement, shown in the diagram below, to demonstrate the principle of moderation in a nuclear reactor.



A golf ball of mass 50 g is initially hanging vertically and just touching a hockey ball of mass 150 g. The golf ball is pulled up to the side and released. It has a speed of  $1.3 \text{ m s}^{-1}$  when it collides head-on with the hockey ball. After the collision the balls move in opposite directions with equal speeds of 0.65 m s<sup>-1</sup>.

(i) Calculate the height above its initial position from which the golf ball is released. Assume that there is no air resistance.

height \_\_\_\_\_ m

(2)

(ii) Show that momentum is conserved in the collision and that the collision is perfectly elastic.

(iii) Calculate the percentage of the kinetic energy of the golf ball transferred to the hockey ball during the collision.

	percentage transferred%	
		(2)
(iv)	Explain how this demonstration relates to the moderation process in a reactor a state <b>one</b> way in which the collisions in a reactor differ from the collision in the demonstration.	and
		(2)
60	Name the substance used as the moderator in a pressurised water reactor (DM	

(v) Name the substance used as the moderator in a pressurised water reactor (PWR).

(1) (Total 13 marks)

In stars, helium-3 and helium-4 are formed by the fusion of hydrogen nuclei. As the temperature rises, a helium-3 nucleus and a helium-4 nucleus can fuse to produce beryllium-7 with the release of energy in the form of gamma radiation.

The table below shows the masses of these nuclei.

Nucleus	Mass / u
Helium-3	3.01493
Helium-4	4.00151
Beryllium-7	7.01473

(a) (i) Calculate the energy released, in J, when a helium-3 nucleus fuses with a helium-4 nucleus.

energy released \_\_\_\_\_\_ J

(ii) Assume that in each interaction the energy is released as a single gamma-ray photon.

Calculate the wavelength of the gamma radiation.

wavelength \_\_\_\_\_ m

(3)

(4)

- (b) For a helium-3 nucleus and a helium-4 nucleus to fuse they need to be separated by no more than  $3.5 \times 10^{-15}$  m.
  - (i) Calculate the minimum total kinetic energy of the nuclei required for them to reach a separation of  $3.5 \times 10^{-15}$  m.

total kinetic energy \_\_\_\_\_\_ J

- (3)
- (ii) Calculate the temperature at which two nuclei with the average kinetic energy for that temperature would be able to fuse.
   Assume that the two nuclei have equal kinetic energy.

temperature \_\_\_\_\_ K

- (c) Scientists continue to try to produce a viable fusion reactor to generate energy on Earth using reactors like the Joint European Torus (JET). The method requires a plasma that has to be raised to a suitable temperature for fusion to take place.
  - (i) State **two** nuclei that are most likely to be used to form the plasma of a fusion reactor.
    - 1.

       2.

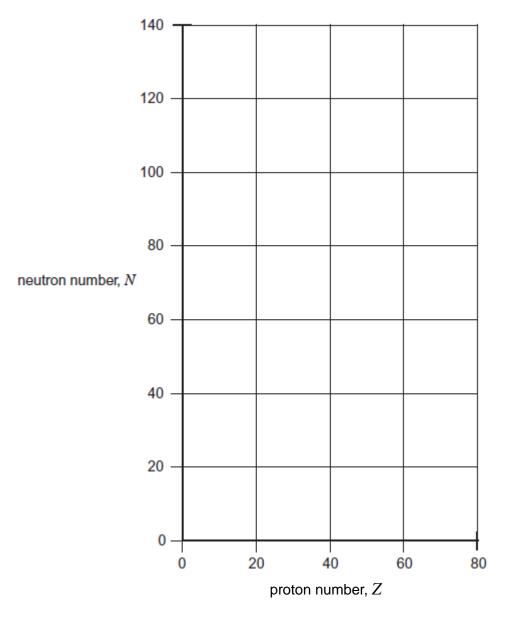
(ii) State **one** method which can be used to raise the temperature of the plasma to a suitable temperature. (1) (Total 16 marks) State what is meant by the binding energy of a nucleus. (a) 10 (2) (i) When a  $\frac{235}{92}$  U nucleus absorbs a slow-moving neutron and undergoes fission one (b) possible pair of fission fragments is technetium  ${}^{112}_{43}$ Tc and indium  ${}^{122}_{49}$ In. Complete the following equation to represent this fission process.  ${}^{1}_{0}n + {}^{235}_{92}U \rightarrow {}^{112}_{43}Tc + {}^{122}_{49}In + \dots$ (1) Calculate the energy released, in MeV, when a single  $^{235}_{92}U$  nucleus undergoes (ii) fission in this way. binding energy per nucleon of  $^{235}_{92}$  U = 7.59 MeV binding energy per nucleon of  ${}^{112}_{43}$ Tc = 8.36 MeV binding energy per nucleon of  $\frac{122}{49} In$  = 8.51 MeV

energy released \_\_\_\_\_ MeV

(iii) Calculate the loss of mass when a  $\frac{235}{92}$ U nucleus undergoes fission in this way.

loss of mass \_\_\_\_\_ kg

(c) (i) On the figure below sketch a graph of neutron number, N, against proton number, Z, for stable nuclei.



(1)

With reference to the figure, explain why fission fragments are unstable and explain (ii) what type of radiation they are likely to emit initially. (3) (Total 12 marks) The carbon content of living trees includes a small proportion of carbon-14, which is a radioactive 11 isotope. After a tree dies, the proportion of carbon-14 in it decreases due to radioactive decay. (a) (i) The half-life of carbon-14 is 5740 years. Calculate the radioactive decay constant in yr<sup>-1</sup> of carbon-14. decay constant \_\_\_\_\_ \_ yr<sup>-1</sup> (1) (ii) A piece of wood taken from an axe handle found on an archaeological site has 0.375 times as many carbon-14 atoms as an equal mass of living wood. Calculate the age of the axe handle in years.

age \_\_\_\_\_ yr

	(b)	Sug	gest why the method of carbon dating is likely to be unreliable if a sample is:	
		(i)	less than 200 years old,	_
		(ii)	more than 60 000 years old.	-
				- (2)
12	(a)	(i)	Define the atomic mass unit.	Total 6 marks)
				- (1)
		(ii)	State and explain how the mass of a ${}_{2}^{4}$ He nucleus is different from the total mits protons and neutrons when separated.	ass of
				-

(b) Explain why nuclei in a star have to be at a high temperature for fusion to take place.

(c) (i) In massive stars, nuclei of hydrogen  ${}_{1}^{1}H$  are processed into nuclei of helium  ${}_{2}^{4}He$  through a series of interactions involving carbon, nitrogen and oxygen called the CNO cycle.

Complete the nuclear equations below that represent the last two reactions in the series.

$$^{\text{mag}}_{8}\text{O} \rightarrow ^{15}_{7}\text{N} + \dots + v_{e}$$

$$^{15}_{7}\mathrm{N} + ^{1}_{1}\mathrm{H} \rightarrow ^{----}_{6}\mathrm{C} + ^{4}_{2}\mathrm{He}$$

(ii) The whole series of reactions is summarised by the following equation.

$$4^{1}_{1}H \rightarrow {}^{4}_{2}He + 2e^{+} + 2v_{e}$$

Calculate the energy, in Me V, that is released.

nuclear mass of  ${}_{2}^{4}$ He = 4.00150 u

energy \_\_\_\_\_ Me V

(3) (Total 12 marks)

**13** (a) Describe the changes made inside a nuclear reactor to reduce its power output and explain the process involved.

(2)

(b) State the main source of the highly radioactive waste from a nuclear reactor.

(1)

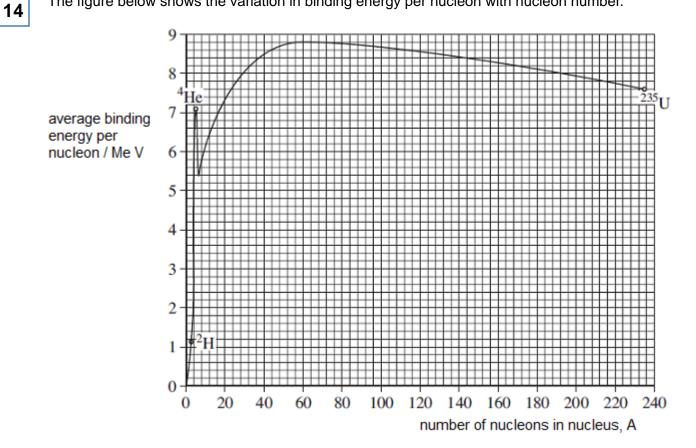
- (c) In a nuclear reactor, neutrons are released with high energies. The first few collisions of a neutron with the moderator transfer sufficient energy to excite nuclei of the moderator.
  - (i) Describe and explain the nature of the radiation that may be emitted from an excited nucleus of the moderator.

(2)

(ii) The subsequent collisions of a neutron with the moderator are elastic.

Describe what happens to the neutrons as a result of these subsequent collisions with the moderator.

(2) (Total 7 marks)



A uranium-235, <sup>235</sup>U, nucleus fissions into two approximately equally sized products. Use (a) data from the graph to show that the energy released as a result of the fission is approximately  $4 \times 10^{-11}$  J.

Show on the graph how you have used the data.

(4)

(b) Using the data below, show that the energy available from the fusion of two hydrogen-2,<sup>2</sup>H, nuclei to make a helium-4,<sup>4</sup>He, nucleus is approximately  $3.7 \times 10^{-12}$  J.

mass of  ${}^{2}H = 2.0135 \text{ u}$ mass of  ${}^{4}He = 4.0026 \text{ u}$ 

(c) Compare the energy available from the complete fission of 1 kg of uranium-235 with the energy available from the fusion of 1 kg of hydrogen-2.

(3)

(d) Fission and fusion reactions release different amounts of energy. Discuss other reasons why it would be preferable to use fusion rather than fission for the production of electricity, assuming that the technical problems associated with fusion could be overcome.

> (2) (Total 13 marks)

- **15** The isotope of uranium,  $\frac{238}{92}$  U, decays into a stable isotope of lead,  $\frac{206}{82}$  Pb, by means of a series of  $\alpha$  and  $\beta^-$  decays.
  - (a) In this series of decays,  $\alpha$  decay occurs 8 times and  $\beta^-$  decay occurs *n* times. Calculate *n*.

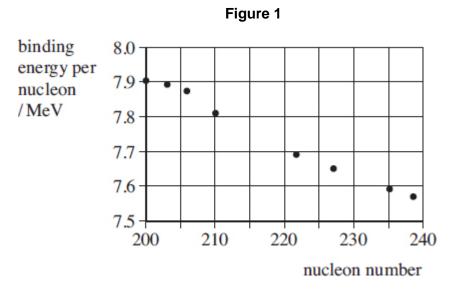
answer = \_\_\_\_\_

(1)

(2)

(b) (i) Explain what is meant by the binding energy of a nucleus.

(ii) **Figure 1** shows the binding energy per nucleon for some stable nuclides.



Use Figure 1 to estimate the binding energy, in MeV, of the  $^{206}_{\phantom{1}82}\mathrm{Pb}\,$  nucleus.

answer = \_\_\_\_\_ MeV

(1)

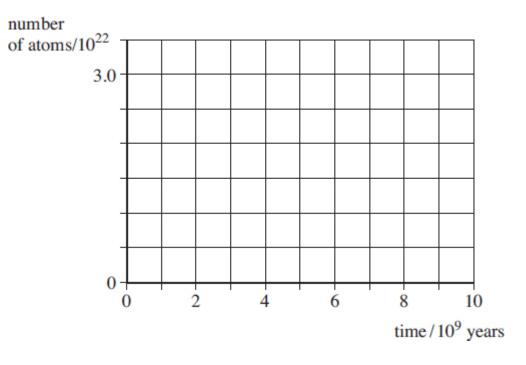
(c) The half-life of  $\frac{238}{92}$  U is 4.5 × 10<sup>9</sup> years, which is much larger than all the other half-lives of the decays in the series.

A rock sample when formed originally contained 3.0 × 10<sup>22</sup> atoms of  $^{238}_{92}$  U and no  $^{206}_{82}$  Pb atoms.

At any given time most of the atoms are either  $^{238}_{92}$  U or  $^{206}_{82}$  Pb with a negligible number of atoms in other forms in the decay series.

(i) Sketch on **Figure 2** graphs to show how the number of  $^{238}_{92}$  U atoms and the number of  $^{206}_{82}$  Pb atoms in the rock sample vary over a period of  $1.0 \times 10^{10}$  years from its formation.

Label your graphs U and Pb.





(ii) A certain time, *t*, after its formation the sample contained twice as many  $^{238}_{92}$  U atoms as  $^{206}_{82}$  Pb atoms.

Show that the number of  $\frac{238}{92}$  U atoms in the rock sample at time *t* was 2.0 × 10<sup>22</sup>.

(ii) Calculate *t* in years.

answer = \_\_\_\_\_ years

(3) (Total 10 marks)

(1)

(a) In a radioactivity experiment, background radiation is taken into account when taking corrected count rate readings in a laboratory. One source of background radiation is the rocks on which the laboratory is built. Give two other sources of background radiation.

source 1 _	 	
source 2 _	 	

(b) A  $\gamma$  ray detector with a cross-sectional area of 1.5 × 10<sup>-3</sup> m<sup>2</sup> when facing the source is placed 0.18 m from the source.

A corrected count rate of 0.62 counts  $s^{-1}$  is recorded.

(i) Assume the source emits  $\boldsymbol{\gamma}$  rays uniformly in all directions. Show that the ratio

number of  $\gamma$  photons incident on detector number of  $\gamma$  photons produced by source

is about 4 ×  $10^{-3}$ .

(ii) The γ ray detector detects 1 in 400 of the γ photons incident on the facing surface of the detector.
 Calculate the activity of the source. State an appropriate unit.

answer = \_\_\_\_\_ unit \_\_\_\_\_

(c) Calculate the corrected count rate when the detector is moved 0.10 m further from the source.

answer = \_\_\_\_\_ counts s<sup>-1</sup>

(3) (Total 9 marks)

17
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The Sun's energy is produced by the fusion of protons. Near the Sun's surface the protons have a mean kinetic energy of 0.75 eV which is too low for fusion to take place. The core, however, has a temperature of about  $1.5 \times 10^6$  K and a pressure of about  $1.0 \times 10^{16}$  Pa. This core consists of a plasma of (mainly) protons. Within the core the density, pressure and temperature of the proton plasma are sufficiently high for nuclear fusion to occur.

The energy is thought to be produced mainly by a cycle called the hydrogen cycle. The overall effect in one cycle is that 4 protons fuse to form a helium nucleus. The total mass of hydrogen that fuses each second is  $7.0 \times 10^{11}$  kg of which about  $5.0 \times 10^9$  kg per second is converted into energy that is radiated.

When answering the following questions assume, where necessary, that the plasma behaves like an ideal gas.

(a) (i) Use the mean value of the kinetic energy of protons near the Sun's surface to calculate the temperature near its surface.

temperature near the Sun's surface \_\_\_\_\_ K

(ii) Calculate the closest distance of approach for two protons near the Sun's surface.

closest distance of approach \_\_\_\_\_ m

(3)

(3)

(iii) Explain why fusion cannot occur near the surface.

(b) (i) Calculate the number of protons in each cubic metre of the Sun's core.

number of protons \_\_\_\_\_

(ii) Calculate the density of the Sun's core.

density of the Sun's core \_\_\_\_\_ kg m  $^{-3}$ 

(c) (i) Show that the data given in the passage in question (a) suggest that every second, about  $4 \times 10^{38}$  protons fuse to form helium nuclei.

(ii) The total binding energy of a helium nucleus is  $4.5 \times 10^{-12}$  J. Determine with an appropriate calculation whether the mass that is converted into radiant energy, stated in the passage, is consistent with this value.

> (4) (Total 20 marks)

(2)

nucleus	binding energy per nucleon/10 <sup>–12</sup> J
helium-4	1.1332417
beryllium-8	1.1314027

- (a) (i) Explain what is meant by the total binding energy of a nucleus.
  - (ii) It is more usual to quote binding energies of nucleons in MeV rather than J. Calculate the total binding energy, in MeV, of a beryllium-8 nucleus.

binding energy \_\_\_\_\_MeV

(b) (i) Calculate the change in mass that occurs when two helium-4 nuclei fuse to form a beryllium-8 nucleus.

mass change \_\_\_\_\_kg

(2)

(1)

(3)

(ii) Two helium-4 nuclei are initially separated by a large distance and are travelling toward one another. The helium nuclei become influenced by the strong force when their centres are separated by a distance of 3.82 × 10<sup>-15</sup> m. Calculate the total initial kinetic energy of the nuclei needed for them to reach this separation.

kinetic energy \_\_\_\_\_J

(iii) Explain why the kinetic energy calculated in part (b)(ii) will not enable the helium nuclei to fuse and produce a beryllium-8 nucleus.

(3) (Total 12 marks)

(3)

In a nuclear reactor the mean energy produced by each uranium-235 nucleus that undergoes induced fission is  $3.0 \times 10^{-11}$  J. In one pressurised water reactor, PWR, the fuel rods in the reactor contain  $2.0 \times 10^4$  kg of uranium-235 and 40% of the energy produced per second is converted to 500 MW of electrical output power. It is assumed that all the energy produced in the reactor core is removed by pressurised water in the coolant system. The pressure of the water is approximately 150 times greater than normal atmospheric pressure. The water enters the reactor at a temperature of 275 °C ad leaves at a temperature of 315 °C. Under the operational conditions of the reactor the mean density of water in the coolant circuit is 730 kg m<sup>-3</sup> and the specific heat capacity of water is approximately 5000 J kg<sup>-1</sup> K<sup>-1</sup>.

normal atmospheric pressure =  $1.0 \times 10^5$  Pa molar mass of uranium-235 = 0.235 kg

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(a) The equation below gives one induced fission reaction that takes place in a reactor.

$$^{235}_{92}$$
U +  $^{1}_{0}$ X  $\Rightarrow ^{n}_{56}$ Br +  $^{90}_{p}$ Kr +  $^{1}_{0}$ X

- (i) State the name of the particle represented by **X**.
- (ii) State the proton and nucleon numbers represented by *p* and *n*.

p	
n	

(b) (i) Calculate the number of fission reactions that occur in the reactor each second.

number of fission reactions per second \_\_\_\_\_

(2)

(1)

(2)

(ii) The reactor fuel rods contain 2.0 × 10<sup>4</sup> kg of uranium-235. Assume that all this uranium-235 could be used.
 Calculate the maximum time, in years, for which the reactor could operate.

the uranium-235 in the re	(r
	actor ruer rods.
	d water on each square ce

force \_\_\_\_\_N

(2)

(d) Calculate, in m<sup>3</sup> s<sup>-1</sup>, the flow rate of the water through the PWR reactor.
 You will need to use data from the passage at the beginning of the question.

(c)

flow rate \_\_\_\_\_  $m^3 s^{-1}$ 

(e) In a PWR the cooling water also acts as the moderator in the reactor and boron rods are used to control the power output. Describe the physical processes that take place in the moderator and control rods.

	(4)
ſ	(•) Total 21 marks)

20

The fissile isotope of uranium,  $\frac{233}{92}$  U, has been used in some nuclear reactors. It is normally produced by neutron irradiation of thorium-232. An irradiated thorium nucleus emits a  $\beta^-$  particle to become an isotope of protactinium.

This isotope of protactinium may undergo  $\beta^-$  decay to become  $\frac{233}{92} \cup$ .

(a) Complete the following equation to show the  $\beta^-$  decay of protactinium.

 $\frac{1}{233} \mathsf{Pa} \rightarrow \frac{233}{92} \mathsf{U}_{+} \beta^{-} + \dots$ 

(2)

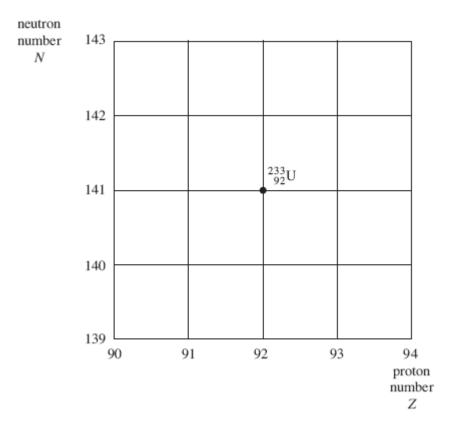
(b) Two other nuclei, **P** and **Q**, can also decay into  $\frac{233}{92} \cup$ .

**P** decays by  $\beta^+$  decay to produce  $\frac{233}{92} \cup$ .

 ${\bf Q}$  decays by  $\alpha$  emission to produce  $\frac{233}{92}\,\cup\,.$ 

The figure below shows a grid of neutron number against proton number with the position of the  $^{233}_{92}$  U isotope shown.

On the grid label the positions of the nuclei **P** and **Q**.



(c) A typical fission reaction in the reactor is represented by

$${}^{233}_{92}$$
U +  ${}^{1}_{0}$ n  $\rightarrow {}^{91}_{36}$ Kr +  ${}^{139}_{56}$ Ba + x neutrons

(i) Calculate the number of neutrons, *x*.

answer = \_\_\_\_\_neutrons

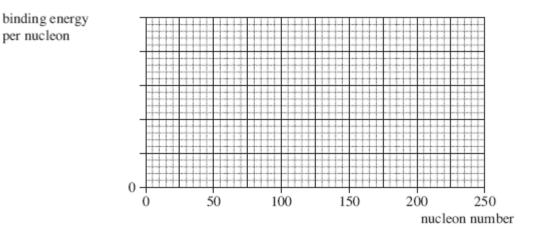
(ii) Calculate the energy released, in MeV, in the fission reaction above.

mass of neutron = 1.00867 u mass of  $^{233}_{92}$   $\cup$  nucleus = 232.98915 u mass of  $^{91}_{36}$  Kr nucleus = 90.90368 u mass of  $^{139}_{56}$  Ba nucleus = 138.87810 u

answer = \_\_\_\_\_MeV

(3) (Total 8 marks) (a) Sketch a graph of binding energy per nucleon against nucleon number for the naturally occurring nuclides on the axes given in the figure below. Add values and a unit to the binding energy per nucleon axis.

21



(4)

(b) Use the graph to explain how energy is released when some nuclides undergo fission and when other nuclides undergo fusion.



Radioisotope thermoelectric generators (RTGs) are electrical generators powered by radioactive decay. As a radioisotope decays some of the energy released is converted into electricity by means of devices called thermocouples. In this way RTGs have been used as power sources in satellites, space probes and heart pacemakers.

The Cassini space probe was launched in 1997. It carried three RTGs each containing 11 kg of a nuclear fuel, plutonium oxide (a compound having two oxygen atoms combined with every plutonium-238 atom). In 1997, when the probe was launched, the power released from one gram of plutonium oxide was 500 mW.

Plutonium-238  $^{238}_{94}$  Pu is an alpha emitter, decaying into uranium(U). The half-life of the decay is 87.7 years.

mass of one mol of plutonium-238 = 238 g mass of one mol of oxygen atoms = 16 g

22

(a) State and explain why environmentalists might have been concerned by the use of such a large quantity of plutonium-238.

(b) State and explain whether the activity of a given number of atoms of plutonium is affected when they are in the form of plutonium oxide.

(c) (i) Calculate the decay constant, in  $s^{-1}$ , for plutonium-238.

decay constant \_\_\_\_\_

s<sup>-1</sup>

(2)

(2)

(I	ii)	Calculate the number of plutonium-238 atoms in the total mass of the plutonium of in the Cassini probe at the beginning of its mission.	
		number of plutonium-238 atoms	
(i	iii)	Calculate the initial activity of the plutonium-238 in the Cassini probe. Give a suitable unit for your answer.	
		initial activity of plutonium-238 unit	
(i	(i)	Write a nuclear equation for the $\binom{238}{94}$ Pu decay.	

(2)

		(ii)	Assume the power released by the RTGs' fuel originated as the kinetic energy of	f the
			alpha particles emitted in the decay of $\binom{238}{94}$ Pu).	
			Calculate the maximum kinetic energy of each alpha particle.	
			kinetic energy of alpha particle J	
			(То	(4) tal 20 marks)
23	A nuc	clide o	of manganese $\left({}^{52}_{25}{ m Mn} ight)$ undergoes beta <sup>+</sup> decay to form a nuclide of chromium (Cr)	).
	(a)	Com	plete the equation for this decay process.	
		52 25	$Mn \to \underbrace{Cr}_{24} Cr + \underbrace{\beta^{+}}_{44} Cr$	(2)
	(b)	State	e the name of the exchange particle involved in this beta <sup>+</sup> decay.	(2)
	\/			
			(T	(1) otal 3 marks)

The age of an ancient boat may be determined by comparing the radioactive decay of  ${}_{6}^{14}$ C from living wood with that of wood taken from the ancient boat.

A sample of  $3.00 \times 10^{23}$  atoms of carbon is removed for investigation from a block of living wood. In living wood one in  $10^{12}$  of the carbon atoms is of the radioactive isotope  ${}^{14}_{6}$ , which has a *decay constant* of  $3.84 \times 10^{-12}$  s<sup>-1</sup>.

(a) What is meant by the decay constant?

(b) Calculate the half-life of <sup>14</sup><sub>6</sub><sup>C</sup> in years, giving your answer to an appropriate number of significant figures.

 $1 \text{ year} = 3.15 \times 10^7 \text{ s}$ 

answer = \_\_\_\_\_ years

(3)

(1)

(c) Show that the rate of decay of the  ${}^{14}_{6}$ <sup>C</sup> atoms in the living wood sample is 1.15 Bq.

(d) A sample of  $3.00 \times 10^{23}$  atoms of carbon is removed from a piece of wood taken

from the ancient boat. The rate of decay due to the  ${}^{14}_{6}$ <sup>C</sup> atoms in this sample is 0.65 Bq. Calculate the age of the ancient boat in years.

answer = \_\_\_\_\_ years

- (3)
- (e) Give **two** reasons why it is difficult to obtain a reliable age of the ancient boat from the carbon dating described.

(2) (Total 11 marks) **25** (a)  $^{212}_{83}$  Bi can decay into  $^{208}_{82}$  Pb by a  $\beta^-$  followed by an  $\alpha$  decay, or by an  $\alpha$  followed by a  $\beta^-$  decay. One or more of the following elements is involved in these decays:

80 Hg , 81 Tl , 84 Po , 85 At .

Write out decay equations showing each stage in both of these decays.

First decay path	Second decay path

(6)

(b) (i) Describe how you would perform an experiment that demonstrates that gamma radiation obeys an inverse square law.

Explain why gamma radiation obeys an inverse square law but alpha and beta (ii) radiation do not. (9) (Total 15 marks) When a nucleus of uranium -235 fissions into barium -141 and krypton -92, the change in (a) 26 mass is 3.1 × 10<sup>-28</sup> kg. Calculate how many nuclei must undergo fission in order to release 1.0 J of energy by this reaction. (2) A nuclear power station produces an electrical output power of 600 MW. If the overall (b) efficiency of the station is 35%, calculate the decrease in the mass of the fuel rods, because of the release of energy, during one week of continuous operation.

> (4) (Total 6 marks)

27	(a)	Calculate the radius of the $\frac{238}{92}$ U nucleus.	
----	-----	---	--

 $r_0 = 1.3 \times 10^{-15} \text{ m}$ 

(b) At a distance of 30 mm from a point source of  $\mathscr{V}$  rays the corrected count rate is *C*. Calculate the distance from the source at which the corrected count rate is 0.10 *C*, assuming that there is no absorption.

(c) The activity of a source of b particles falls to 85% of its initial value in 52 s. Calculate the decay constant of the source.

(2)

(2)

(d) Explain why the isotope of technetium, <sup>99</sup>Tc <sub>m</sub>, is often chosen as a suitable source of radiation for use in medical diagnosis.

You may be awarded additional marks to those shown in brackets for the quality of written communication in your answer.



**28** In a geothermal power station, water is pumped through pipes into an underground region of hot rocks. The thermal energy of the rocks heats the water and turns it to steam at high pressure. The steam then drives a turbine at the surface to produce electricity.

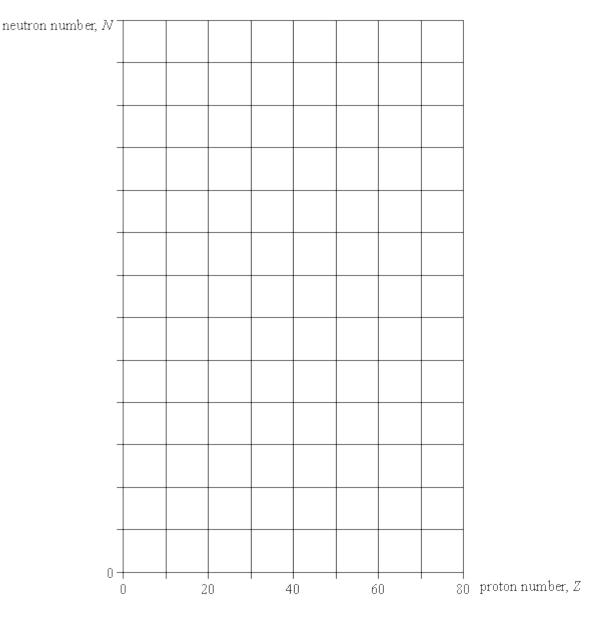
- (a) Water at 21°C is pumped into the hot rocks and steam at 100°C is produced at a rate of 190 kg s<sup>-1</sup>.
  - (i) Show that the energy per second transferred from the hot rocks to the power station in this process is at least 500 MW.

specific heat capacity of water =  $4200 \text{ J kg}^{-1} \text{ K}^{-1}$ specific latent heat of steam =  $2.3 \times 10^6 \text{ J kg}^{-1}$  (ii) The hot rocks are estimated to have a volume of  $4.0 \times 10^6$  m<sup>3</sup>. Estimate the fall of temperature of these rocks in one day if thermal energy is removed from them at the rate calculated in part (i) without any thermal energy gain from deeper underground.

	specific heat capacity of the rocks = $850 \text{ J kg}^{-1} \text{ K}^{-1}$ density of the rocks = $3200 \text{ kg m}^{-3}$
Ge	othermal energy originates as energy released in the radioactive decay of the
ura	anium isotope 238 U deep inside the Earth. Each nucleus that decays releases 4.2 Me
Ca	lculate the mass of $\frac{238}{92}$ U that would release energy at a rate of 500 MW.
	If-life of $^{238}_{92}$ U = 4.5 × 10 <sup>9</sup> years
mo	blar mass of $^{238}_{92}$ U = 0.238 kg mol <sup>-1</sup>

(7)

(a) Sketch, using the axes provided, a graph of neutron number, *N*, against proton number, *Z*, for stable nuclei over the range Z = 0 to Z = 80. Show suitable numerical values on the *N* axis.



(2)

- (b) On the graph indicate, for each of the following, a possible position of a nuclide that may decay by
  - (i)  $\alpha$  emission, labelling the position with **W**,
  - (ii)  $\beta^-$  emission, labelling the position with **X**,
  - (iii)  $\beta^+$  emission, labelling the position with **Y**.

(3)

(c)	The isotope $\frac{222}{86}$ Rn decays sequentially by emitting $\alpha$ particles and $\beta^{-}$ particles, eventually forming the isotope $\frac{206}{82}$ Pb. Four $\alpha$ particles are emitted in the sequence.	
	Calculate the number of $\beta^-$ particles in the sequence.	
		(2)
(d)	A particular nuclide is described as proton-rich. Discuss <b>two</b> ways in which the nuclic decay. You may be awarded marks for the quality of written communication in your as	
	<i></i>	(3)
		tal 10 marks)
(a)	Suggest <b>two</b> reasons why an $\alpha$ particle causes more ionisation than a $\beta$ particle of th same initial kinetic energy.	e
	You may be awarded marks for the quality of written communication in your answer.	

(2)

- (b) A radioactive source has an activity of  $3.2 \times 10^9$  Bq and emits  $\alpha$  particles, each with kinetic energy of 5.2 Me V. The source is enclosed in a small aluminium container of mass  $2.0 \times 10^{-4}$  kg which absorbs the radiation completely.
  - (i) Calculate the energy, in J, absorbed from the source each second by the aluminium container.

(ii) Estimate the temperature rise of the aluminium container in **1 minute**, assuming no energy is lost from the aluminium.

specific heat capacity of aluminium = 900 J kg<sup>-1</sup> K<sup>-1</sup>

(5) (Total 7 marks)

## Mark schemes

1

(i) momentum (= E/c) (a)  $= 5.94 \times 10^{-11} / 3.00 \times 10^8 = 2.0 \times 10^{-19} (\text{kg m s}^{-1})$  $(= 1.98 \times 10^{-19} \text{ kg m s}^{-1})$ Or evidence of use of  $E = hc / \lambda \checkmark$  $\lambda = (h / mv = 6.63 \times 10^{-34} / 1.98 \times 10^{-19}) = 3.35 \times 10^{-15} \text{ (m)}$ (allowable range  $3.32 \times 10^{-15} - 3.37 \times 10^{-15}$  m)  $3.348 \times 10^{-15}$  m alone may score 1 mark A completed calculation to at least 3 sf must be seen for 2nd mark 2 nuclear radius = 0.61  $\lambda$  / sin  $\theta$  = 0.61 x 3.35 x 10<sup>-15</sup> / sin 42° (ii) =  $3.1 \times 10^{-15}$  (m)  $\checkmark$  (allow  $2.95 - 3.1 \times 10^{-15}$  m which is a range incorporating  $3.32 \times 10^{-15} - 3.37 \times 10^{-15}$  m and  $42^{\circ} - 43^{\circ}$ ) (The answer must be to 2 sf or better

note  $3.3 \times 10^{-15}$ , 42° gives  $3.008 \times 10^{-15}$  m i.e.  $3.0 \times 10^{-15}$ )

(b) (i) diagram to show a labelled α source, foil target and detector (which is not simply a forward facing screen so there must be some indication it can move around the target e.g. a curved arrow / positioned at an angle / or screen curved round target or detectors shown in at least two positions) √

with evacuated vessel or an item to collimate the beam  $\checkmark$  (the evacuated vessel does not have to be drawn so a simple label of 'in a vacuum' will gain the mark.) (A tube or a plate(s) must be drawn with a collimator label or a label on an emergent alpha beam from the drawn item (which is distinct from the source) will gain a mark)

'detector' has alternatives e.g. fluorescent screen / scintillator / zinc sulphide

2

1

(ii) The mark scheme for this part of the question includes an overall assessment for the Quality of Written Communication (QWC).

## Descriptor

### High Level – Good to Excellent

Both observations should be given ie most  $\alpha$  particles pass straight through the foil and that some  $\alpha$ 's are backscattered. Again both of these must be explained. Additionally one approach to finding the upper limit to the radius must be given and interpreted.

The information presented as a whole should be well organised using appropriate specialist vocabulary. There should only be one or two spelling or grammatical errors for this mark.

6 marks = all 3 bullet points covered in full. 5 marks = Same as 6 marks but one explanation is omitted or poorly expressed

5 - 6

#### Intermediate Level – Modest to Adequate

Both observations should be given ie most  $\alpha$  particles pass straight through the foil and that some  $\alpha$ 's are backscattered. Both of these observations can be explained or one of them explained along with the observation necessary to obtain the upper limit to the nuclear radius but without the explanation of how to use the data.

The grammar and spelling may have a few shortcomings but the ideas must be clear.

4 marks = for first two bullet points covered in full.

Alternatively both observations given but only one explained along with an observation necessary to find the upper limit to the nuclear radius.

3 marks = for both observations given but only one explained

3 - 4

#### Low Level – Poor to Limited

Any two observations or interpretations but an interpretation must come with the appropriate observation.

There may be many grammatical and spelling errors and the information may be poorly organised.

2 marks for two observations or one observation along with its interpretation.

1 mark = Any observation..

1 - 2

#### The description expected in a competent answer should include:

- 1. most  $\alpha$  particles pass straight through
- 2. which suggests an atom is composed of mainly open space
- 3.  $\alpha$  particles can be backscattered or scattered by more than 90°
- 4. which suggests
- i. they have collided with something more massive than themselves (using momentum considerations)
- ii. they have been repelled by a concentrated positive charge (using coulomb repulsion)
  - these together suggest a 'solar system' configuration for the atom.
- 5. Consider the proportion of  $\alpha$ 's passing straight through the foil, i.e. how much of the straight through beam is stopped by the foil.
- Or

Appreciate that scattering of  $\alpha$ 's close to 180° takes place which means the  $\alpha$ 's have not touched the nuclear surface.

6. First alternative data can be related to how much of the beam is intercepted by nuclei. Using the number of atomic layers / thickness of foil and the nuclear cross-sectional area the upper limit to the radius may be found

Or If second alternative is used some detail is needed to gain this point. Either a discussion of the loss KE = gain PE to find upper limit to the radius Or the idea that backscattering is not observed / falls off if the alpha comes close to the nucleus because the strong nuclear force (SNF) takes over and so provides an upper limit to the radius.

### (owtte)

Do not award 'large space between atoms'.

The question is a QWC and not all the points are expected to be given as detailed on the left. This check list gives a brief idea of the main parts expected.

(note the pairing of 1 and 2, 3 and 4, 5 and 6 where the second of each pair cannot be given in isolation but the first of each pair does not have to perfect)

If it is obvious the candidate is talking about an alpha particle but calls it something different do not over penalise. E.g. miss out a pairing of marks then mark as if alpha)

Quick check list.

- 1. Most alpha's go straight on
- 2. Because an atom has mainly empty space
- 3. A few alpha's are backscattered
- 4. Because of nuclear positive charge or large nuclear mass

5. Method suggested to find R (drop in straight on beam Or backscattering means  $\alpha$ 's have not touched nucleus)

6. Some detail such as ref. to (nuclear) area <u>and</u> (foil) thickness Or alpha KE to PE giving r Or if  $\alpha$ 's touch surface SNF stops scattering.

[11]

(a) nuclear fallout / testing / weapons / nuclear accidents / Chernobyl / nuclear waste / nuclear medicine / X-rays / specific uses of radioactive sources eg medical tracers CT scan etc. / cosmic rays as a result of air travel ✓

(Any source of radiation that an individual may encounter which would not have existed 100 years ago)

No mark for general answers such as 'medical' or Nuclear Power / nuclear plant.

If a list is given all must be correct but ignore generalisations such as medical or nuclear power.

(b) (i)  $/_{15CCR} = 2050 - 40 = 2010 \checkmark$ 

Use of inverse square law eg  $I_{CCR90} = I_{CCR15} \left(\frac{d_{15}}{d_{90}}\right)^2 \sqrt{(0.15 / 0.90)^2} = 55.8$ 

 $I_{90CR} = 55.8 + 40$ 

 $I_{90CR}$  = 96 counts min<sup>-1</sup>  $\checkmark$ 

regardless of order: 1st mark subtraction of background in original data 2nd mark is for using inverse square function 3rd mark is for the answer

(ii) (reduce impact of) random error / decrease the (percentage) uncertainty / improve the statistics (because the percentage error is proportional to the inverse square-root of the count) √ (owtte)

The answer must be an uncertainty related statement and not increases reliability / accuracy or increased chance of a reading (although these ideas can accompany a correct answer) Ignore comparisons with the background count.

1

3

(iii) use (sensible) absorber between source and detector ✓ (sensible absorber means it must have a noticeable effect e.g. 1mm of metal / aluminium sheet / 5mm perspex but do not allow metal foil / paper sheets. Also its effect must not be so great that it reduces the gamma rays noticeably)

(These two marks are independent)

3

 $\beta$  shown by count rate falling when sheet of aluminium absorber is used  $\checkmark$  Or (using the existing apparatus)

Compare the results (at various distances) in air with the expected inverse square law  $\checkmark$ 

Below the range of beta law does not work but above range it does.  $\checkmark$ 

2nd mark no mark given if count rate falls to zero as  $\gamma$  is still present (magnetic deflection is not common but if seen.

Use of magnetic deflection  $\checkmark$  correct deflection of beta from the beam  $\checkmark$ )

(If a cloud chamber is suggested. Observe the tracks in a cloud chamber  $\checkmark$  beta tracks have varying lengths or they are curly / not straight  $\checkmark$ 

(The value of the range of beta is not a marking point so accept 15 – 80 cm if a number is given)

[7]

2

(a) (i) Fission occurs at A values above the peak / above A of about 56 and fusion occurs at A values below the peak / below A of about 56  $\checkmark$ 

Fission is the splitting of a nucleus (into two smaller ones) and fusion is the joining of two nuclei  $\checkmark$ 

First mark uses the graph so 'fission occurs in very large nuclei' does not gain a mark. (allow other interpretations that use the graph eg gradients)

2nd Mark splitting into 2 is not required for fission but if the answer implies something different like the separating of all the nucleons the mark may not be given.

Energy is released when the binding energy (per nucleon) is increased ✓ fusion energy is greater as the increase in BE(/A) for fusion > increase in BE(/A) for fission (owtte) ✓

The last point can be given for a reference to the larger gradient at small values of A (fusion region) compared to the gradient at large values of A (fission region)

2

(b)

(i)

 $\Delta m = (8m_p + 8m_n) - M_{oxygen}$ mark for substituting data into the above equation in any workable consistent units

= 8(1.00867+1.00728) − 15.991 **√** 

(∆*m* = 0.1366 u

 $\Delta m = 0.1366 \times 1.661 \times 10^{-27}$ ) = 2.3 × 10<sup>-28</sup> (kg)  $\checkmark$ 

(range of answers 2.2 - 2.3 ×  $10^{-28}$  kg)

Substitution may take the following form  $8(1.673 \times 10^{-27})+8(1.675 \times 10^{-27})-(15.991 \times 1.661 \times 10^{-27}) \checkmark$   $= 2.23 \times 10^{-28} \text{ (kg) } \checkmark$ Correct answer gains full marks. Look out for a physics error in which u is not taken as  $1.661 \times 10^{-27}$ kg

2

1

- (ii)  $E = m \times c^2 = 2.3 \times 10^{-28} \times (3.00 \times 10^8)^2 = 2.07 \times 10^{-11} \text{ J}$ BE = 2.07 × 10<sup>-11</sup> / 1.6 × 10<sup>-13</sup> = 130 (MeV) ✓ (129 MeV) Or using using  $\Delta m = 0.1366$  u (this must appear in b(i) for this approach) BE = 0.1366 × 931.3 = 130 (MeV) ✓ (127 MeV) *CE is allowed but only if the calculation is shown Note answer* = b(i) × 5.625 × 10<sup>29</sup> *answer only is acceptable for one mark. (factor may be 931 or 931.5)*
- (iii) read from the graph the BE/A for <sup>16</sup><sub>8</sub>O and multiply by the number of nucleons (or 16)
   ✓

Or show the calculation

BE = 8(Mev) × 16(nucleons) = 130 (MeV) ✓ (128 MeV) ✓
There must be a reference to <sup>16</sup>/<sub>8</sub>O position on the graph.
with the calculation allow BE = 8.1(Mev) × 16(nucleons) = 130 (MeV)
A calculation may lead to an answer in joule

[8]

1

(a) (3.0 × 10<sup>-10</sup>/24) × 6.02 × 10<sup>23</sup> seen√

 $(7.52 \times 10^{10})$ 

4

	(b)	Decay constant = $(0.69 / 14.8 h^{-1})$ or $1.3 \times 10^{-5} s^{-1} \checkmark$		
		$A = 1.30 \times 10^{-5} \times 7.5 \times 10^{10} \checkmark$		
		9.75 × 10 <sup>5</sup> Bq √		
		Allow 2 or 3 sf Allow use of $A = \lambda N$ with an incorrectly calculated decay constant	3	
	(c)	Activity 3.5 h later should be A = 9.8 × $10^5 e^{-0.0466 \times 3.5} \checkmark$		
		8.33 × 10 <sup>5</sup> Bq√		
		Volume of liquid = $(8.33 \times 10^5 / 3600) \times 15 = 3470 \text{ cm}^3 \checkmark$	3	
	(d)	Estimate gives 3700 compared with $3500\checkmark$		
		Flask has more mass than average / liquid is not water $\checkmark$	2	
]	(a)	A α particles 🗸		[9]
1		[auto mark question]	1	

(b) (i)

5

type of radiation	Typical range in air / m
α	0.04 🗸
β	0.40 🗸

Allow students to use their own distance units in the table  $\alpha$  allow 0.03  $\rightarrow$  0.07 m  $\beta$  allow 0.20  $\rightarrow$  3.0 m. If a range is given in the table use the larger value.

A specific number is required e.g. not just a few cm.

	(ii)	reference to the inverse square law of ( $\gamma$ radiation) or		
		reference to lowering of the solid angle (subtended by the detector as it moves away)		
		or		
		radiation is spread out (over a larger surface area as the detector is moved away) $\checkmark$		
		(owtte)		
		Ignore any references to other types of radiation.		
		Any contradiction loses the mark. For example, follows inverse		
		square law so intensity falls exponentially.	1	
			I	
(c)	dust	dust may be ingested / taken into the body / breathed in $\checkmark$		
		First mark for ingestion not just on the body		
	00110	ing (malagulag in human tiggua ( galle) to be made cancerous ( killed ( damaged		
		ing (molecules in human tissue / cells) to be <u>made cancerous / killed / damaged</u> nisation √		
		Second mark for idea of <u>damage</u> from <u>ionisation</u>		
		Cocona mark for laba of <u>damago</u> nom <u>iomodilon</u>	2	
				[6]
(a)	(i)	electromagnetic / electrostatic / Coulomb (repulsion between the alpha particles and		
(a)	(1)	the nuclei) $\checkmark$		
		The interaction must be named not just described.		
			1	
	(ii)	the scattering distribution remains the same (because the alpha particles		
	(1)	interact with a nucleus) whose charge / proton number / atomic number		
		remains the same or the (repulsive) force remains the same		
		The mark requires a described distribution and the reason for it.		
		Or the scattering distribution changes / becomes less distinct because there is a		
		mixture of nuclear masses (which gives a mixture of nuclear recoils) $\checkmark$		
		(owtte)		
		A reference must be made to mass and not density or size.		
			1	
(6)		use of graph to find r		
(b)	(i)	use of graph to find $r_0$		
		e.g. $r_0 = 6.0 \times 10^{-15} / 75^{1/3} \sqrt{(0.15 + 10^{-15} / 175^{1/3})}$		
		(or $8.0 \times 10^{-15} / 175^{1/3}$ )		
		$(r_0 = 1.43 \times 10^{-15} \text{ m})$		
		Substitution and calculation t must be shown.		
		Condone a gradient calculation on <u>R against A<sup>1/3</sup> graph</u> (not graph		
		in question) as $R \propto A^{1/3}$	1	
			T	

## (ii) Escalate if clip shows $\frac{27}{13}$ Al in the question giving R $\approx$ 4 × 10<sup>-15</sup> m.

(using  $R = r_0 A^{\frac{1}{3}}$ )  $R = 1.43 \times 10^{-15} \times 51^{1/3} \checkmark$   $R = 5.3 \times 10^{-15} \text{ (m) } \checkmark$   $(R = 5.2 \times 10^{-15} \text{ m from})$   $r_0 = 1.4 \times 10^{-15} \text{ m})$ First mark for working. Second mark for evaluation which must be 2 or more sig figs allow CE from (i)  $R = 3.71 \times (i)$ . **Possible escalation**.

## (c) Escalate if clip shows $\frac{27}{13}$ in the question and / or the use of 27 in the working.

density = mass / volume  $m = 51 \times 1.67 \times 10^{-27}$ (= 8.5 × 10<sup>-26</sup> kg)

Give the first mark for substitution of data into the top line or bottom line of the calculation of density.

```
v = 4/3\pi (5.3 \times 10^{-15})^3
(6.2(4) × 10^{-43} m<sup>3</sup>)
```

(6.2(4) × 10<sup>-43</sup> m<sup>3</sup>)

In the second alternative the mark for the substitution is only given if the working equation is given as well.

#### Or

density =  $A \times u / 4/3\pi (r_0 A^{1/3})^3$ =  $u /4/3\pi (r_0)^3$ 51 × 1.67 × 10<sup>-27</sup> would gain a mark on its own but 1.66 × 10<sup>-27</sup> would need  $u / 4/3\pi (r_0)^3$  as well to gain the mark.

top line =  $1.66 \times 10^{-27}$ 

bottom line =  $4/3\pi (1.43 \times 10^{-15})^3$ 

```
\checkmark for one substitution
```

```
density = 1.4 \times 10^{17} \checkmark
(1.37 × 10<sup>17</sup>)
```

kg m⁻³ √

Expect a large spread of possible answers. For example If  $R = 5 \times 10^{-15}$  V = 5.24 × 10<sup>-43</sup> and density = 1.63 × 10<sup>17</sup>. **Possible escalation**.

3

(a) 
$$\begin{array}{c} 239\\93\end{array}$$
 Np  $\rightarrow \begin{array}{c} 239\\94\end{array}$  Pu +  $\begin{array}{c} (0)\\(-1)\end{array}\beta^{-} + \begin{array}{c} (0)_{\nu}^{-}\sqrt{2}\end{array}$ 

First mark for one anti-neutrino or one beta minus particle in any form e.g. e<sup>-</sup>. If subscript and superscripts are given for these they must be correct but ignore the type of neutrino if indicated. The second mark is for both particles and the rest of the equation. Ignore the full sequence if it is shown but the Np to Pu must be given separately for the mark.

(b) (i)  $T_{1/2} 2.0 \rightarrow 2.1 \times 10^5 \text{ s} \checkmark$ 

then substitute and calculate

 $\lambda = \ln 2 / T_{1/2} \checkmark$ 

 $T_{1/2}$  may be determined from graph not starting at zero time. Look for the correct power of 10 in the half-life – possible AE.

#### Or

(substitute two points from the graph into  $A = A_0 e^{-\lambda t}$ ) e.g. 0.77 × 10<sup>12</sup> = 4.25 × 10<sup>12</sup> exp( $-\lambda \times 5 \times 10^5$ )  $\checkmark$ then make  $\lambda$  the subject and calculate  $\checkmark$ 

(the rearrangement looks like

 $\lambda = [\ln (A_o / A)] / t$ 

or  $\lambda = - [\ln (A / A_o)] / t)$ 

Allow the rare alternative of using the time constant of the decay  $A = A_o \exp(-t/t_{tc})$ from graph  $t_{tc} = 2.9 \rightarrow 3.1 \times 10^5 \text{ s/}$  $\lambda = 1/t_{tc} = 3.4 \times 10^{-6} \text{ s}^{-1} \text{ /}$ No CE is allowed within this guestion.

both alternatives give

 $λ = 3.3 → 3.5 × 10^{-6} s^{-1} √$ For reference  $T_{1/2} = 2.0 × 10^5 s \text{ gives}$   $λ = 3.5 × 10^{-6} s^{-1} and$   $T_{1/2} = 2.1 × 10^5 s \text{ gives}$  $λ = 3.3 × 10^{-6} s^{-1}.$ 

(ii) (using  $A = N\lambda$ 

 $N = 0.77 \times 10^{12} / 3.4 \times 10^{-6} = 2.2(6) \times 10^{17} )$ allow 2.2  $\rightarrow$  2.4 × 10<sup>17</sup> nuclei  $\checkmark$ 

> A possible route is find  $N_o = A_o / \lambda$ then use  $N = N_o e^{-\lambda t}$ . Condone lone answer.

> > 1

2

(c)	(i)	uranium (- 235 captures) a neutron (and splits into 2 smaller nuclei / fissio	n		
		fragments) <u>releasing more neutrons</u> √			
		First mark for uranium + neutron gives more neutrons.			
		Ignore which isotope of uranium is used.			
		(at least one of) these neutrons go on to cause further / more splitting / fissioning (of uranium– 235) $\checkmark$			
		Second mark for released neutron causes more fission.			
		The word 'reaction' may replace 'fission' here provided 'fission /			
		splitting of uranium' is given somewhere in the answer.		2	
	<i>/</i>			-	
	(ii)	Escalate if clip shows critical mass in the question. the moderator slows down / reduces the kinetic energy of <u>neutrons</u> $\checkmark$			
		so neutrons are absorbed / react / fission (efficiently) by the <u>uranium / fuel</u>	$\checkmark$		
		owtte	-		
		Possible escalation.			
				2	
	(iii)	<u>neutrons</u> are absorbed / collide with (by the nuclei in the shielding) $\checkmark$			
		Second mark is only given if neutrons appear somewhere in the answer.			
		converting the nuclei / atoms (of the shielding) into unstable isotopes (owt	te)		
		No neutrons = no marks.			
		Making it neutron rich implies making them unstable.		2	
					[11]
(a)	ANY	2 from			
		<ul> <li>Slow moving neutrons or low (kinetic) energy neutrons</li> </ul>			
			B1		
		• (They are in) thermal equilibrium with the moderator /			
		Are in thermal equilibrium with other material (at a			
		temperature of about 300 K)			
			B1		
		$\mathbf{A}$ Have exercise of order of 0.025 oV			
		<ul> <li>Have energies of order of 0.025 eV</li> </ul>			
		Have (range of) KE similar to that of a gas at 300 K or			
		room temperature		2	

(b)	(i)	Use of $mgh = \frac{1}{2} mv^2$ by substitution or rearranges to make h the subject <i>PE</i> for use of equation of motion (constant acceleration)	
			C1
			CI
		0.086(1) (m) or 0.086(2) (m)	
			A1
	(ii)	Correct equation for conservation of momentum	
	(11)	$m_1u_1 (+ m_2u_2) = m_1v_1 + m_2v_2$	
		or states momentum before = momentum after or p <sub>before</sub> =	
		Pafter	
			B1
		(Correct clear Manipulation =) 0.065 (+ 0) = - 0.0325 + 0.0975	
		or -0.065 (+ 0) = 0.0325 - 0.0975 must see signs	
		Condone non-SI here:	
		65 (+0) = - 32.5 + 97.5	
			B1
		States initial kinetic energy = final kinetic energy or States kinetic energy is conserved	
		Allow equivalent on RHS where masses are summed in	
		one KE term	
			B1
		(Correct clear Manipulation=) 0.04225 = 0.0105625 + 0.0316875	
		Or equivalent workings with numbers seen	
		and 0.04225 = 0.04225 / KE before = KE after	
			B1

(iii)	(Percentage / fraction remaining after 1 collision =) <sup>1</sup> / <sub>4</sub> = 25% seen		
	OR % remaining = $100 \times \frac{1}{2} m(1.3^2 - 0.65^2) / \frac{1}{2} m1.3^2$ or hockey ball = 0.0317 and initial ke = 0.04225 or their KE <sub>hb</sub> / 0.04225 or their KE <sub>hb</sub> / their KE <sub>T</sub>	C1	
	75(%) range 75 to 76		
		A1	2
(iv)	<b>Demonstrates:</b> Slowing down / loss of KE of golf ball is like neutrons slowed down / Neutrons can lose KE by elastic collisions also	B1	2
	Differs: Collisions in a reactor are not always / rarely head-on or KE loss is variable or Collisions are not <u>always</u> elastic or Ratio of mass of neutron to mass of nucleus is usually much smaller in a reactor	ы	
		B1	2
(v)	Water		
		B1	1

[13]

**9** (a)

(i)

(Mass change in u=)  $1.71 \times 10^{-3}$  (u) or (mass Be-7) – (mass He-3) – (mass He-4) seen with numbers

		2.84 × 10 <sup>-30</sup> (kg) <b>or</b> Converts their mass to kg <i>Alternative 2nd mark:</i> <i>Allow conversion of 1.71 × 10<sup>-3</sup> (u) to MeV by</i> <i>multiplying by 931 (=1.59 (MeV))</i> <b>seen</b>	
		Substitution in E = $mc^2$ condone their mass <u>difference</u> in	C1
		this sub but must have correct value for $c^2 (3 \times 10^8)^2$ or $9 \times 10^{16}$ Alternative 3rd mark: Allow their MeV converted to joules (× 1.6 × 10 <sup>-13</sup> ) <b>seen</b>	
			C1
		$2.55 \times 10^{-13}$ (J) to $2.6 \times 10^{-13}$ (J) Alternative 4th mark:	
		Allow 2.5 × 10 <sup>-13</sup> (J) for this method	A1
	(ii)	Use of <i>E=hc / λ <b>ecf</b></i>	
		Correct substitution in rearranged equation with $\lambda$ subject <b>ecf</b>	C1
			C1
		$7.65 \times 10^{-13}$ (m) to $7.8 \times 10^{-13}$ (m) ecf	
(b)	(i)	Use of $E_p$ formula:	A1
			C1
		Correct charges for the nuclei and correct powers of 10	64
		2.6(3) × 10 <sup>−13</sup> J	C1
			A1

4

3

3

C1

		(ii)	Uses K <i>E</i> = 3 / 2 <i>kT</i> : <b>or</b> halves K <i>E</i> <sub>T</sub> , K <i>E</i> = 1.3 × 10 <sup>-13</sup> (J) <b>seen</b> <b>ecf</b>			
				C1		
			Correct substitution of data <b>and</b> makes T subject <b>ecf</b> Or uses KE <sub>T</sub> value <b>and</b> divides T by 2			
				C1		
			6.35 × 10 <sup>9</sup> (K) or 6.4 × 10 <sup>9</sup> (K) or 6.28 × 10 <sup>9</sup> (K) or 6.3 × 10 <sup>9</sup> (K) <b>ecf</b>			
				A1	2	
	<i>.</i> .				3	
	(C)	(i)	Deuteron / deuterium / hydrogen-2			
				B1		
			Triton / tritium / hydrogen-3			
				B1		
					2	
		(ii)	Electrical heating / electrical discharge / inducing a current in plasma / use of e-m radiation / using radio waves (causing charged particles to resonate)			
				B1		
					1	[16]
						[10]
10	(a)	into i (or e	amount of energy required to separate a nucleus $\checkmark$ its separate neutrons and protons / nucleons $\checkmark$ energy released on formation of a nucleus $\checkmark$ its separate neutrons and protons / constituents $\checkmark$ )			
			1 <sup>st</sup> mark is for correct energy flow direction			
			2 <sup>nd</sup> mark is for binding or separating nucleons (nucleus is in the question but a reference to an atom will lose the mark) ignore discussion of SNF etc			
			both marks are independent		2	
	(b)	(i)	$2_0^1 \mathbf{n}$ or ${}_0^1 \mathbf{n} + {}_0^1 \mathbf{n} \checkmark$		2	
			must see subscript and superscripts			
					1	

(ii) binding energy of U = 235 × 7.59 √ ( = 1784 (MeV)) binding energy of Tc and In = 112 × 8.36 + 122 × 8.51 √ (= 1975 (MeV))energy released ( = 1975 – 1784) = 191 (MeV) √ (allow 190 MeV) 1<sup>st</sup> mark is for 235 × 7.59 seen anywhere 2<sup>nd</sup> mark for 112 × 8.36 + 122 × 8.51 or 1975 is only given if there are no other terms or conversions added to the equation (ignore which way round the subtraction is positioned) correct final answer can score 3 marks (iii) energy released  $= 191 \times 1.60 \times 10^{-13} \checkmark$  $(=3.06 \times 10^{-11} \text{ J})$ loss of mass ( =  $E/c^2$  )  $= 2.91 \times 10^{-11} / (3.00 \times 10^8)^2)$  $= 3.4 \times 10^{-28}$  (kg)  $\checkmark$ or  $= 191 / 931.5 \text{ u} \checkmark (= 0.205 \text{ u})$  $= 0.205 \times 1.66 \times 10^{-27}$  (kg)  $= 3.4 \times 10^{-28} (\text{kg}) \checkmark$ allow CE from (ii) working must be shown for a CE otherwise full marks can be given for correct answer only note for CE answer = (ii)  $\times 1.78 \times 10^{-30}$  $(2.01 \times 10^{-27} \text{ is a common answer})$ line or band from origin, starting at 45° up to Z approximately = 20 reading (c) (i)  $Z = 80, N = 110 \rightarrow 130 \checkmark$ initial gradient should be about 1 (ie Z = 20 ; N = 15  $\rightarrow$  25) and overall must show some concave curvature. (Ignore slight waviness in the line) if band is shown take middle as the line

if line stops at N > 70 extrapolate line to N = 80 for marking

1

2

(ii) fission fragments are (likely) to be above / to the left of the line of stability  $\sqrt{}$  fission fragments are (likely) to have a larger N/Z ratio than stable nuclei or

fission fragments are neutron rich owtte  $\checkmark$ 

and become neutron or  $\beta^{\scriptscriptstyle -}$  emitters  $\checkmark$ 

ignore any reference to α emission a candidate must make a choice for the first two marks stating that there are more neutrons than protons is not enough for a mark 1<sup>st</sup> mark reference to graph 2<sup>nd</sup> mark – high N / Z ratio or neutron rich 3<sup>rd</sup> mark beta <u>minus</u> note not just beta

[12]

3

1

11

(a)

(i)

 $(1.21 \times 10^{-4} \text{ yr}^{-1})$ 

only allow  $3.83 \times 10^{-12} \text{ s}^{-1}$  if the unit has been changed working is not necessary for mark

(ii) (use of  $N_t = N_o e^{-\lambda t}$  and activity is proportional to N  $A_t = A_o e^{-\lambda t}$ )  $0.375 = \exp - (1.21 \times 10^{-4} \times t) \checkmark$   $t = \frac{\ln(\frac{1}{0.375})}{1.21 \times 10^{-4}} \checkmark$   $t = 8100 \text{ or } 8200(\text{yr}) \checkmark$   $1^{st}$  mark substitution, allow EC from (i)  $2^{nd}$  mark rearranging, allow EC from (i)

 $\lambda$  ( = ln 2 /  $T_{1/2}$  = 0.693 / 5740 ) = 1.2 × 10<sup>-4</sup> (yr<sup>-1</sup>)  $\checkmark$ 

Allow  $t/T_{1/2} = 2^n$  approach

3<sup>rd</sup> mark no EC (so it is not necessary to evaluate a CE) so max 2 for a CE full marks can be given for final answer alone. A minus in the final answer will lose the last mark

	(b)	the small drop	measure accurately) / change in activity / count-rate ge / drop in the ratio of C-14 to C-12 √	
		or the ratio of or there are to or there is very	-	
			C-14 (in the biosphere) is uncertain (this long ago) $\checkmark$ needs some reference to a change in count-rate or activity	
		for the n		
		in readin activity t suggesti	nt in 2 <sup>nd</sup> mark og a script assume C-14 is the subject. Eg 'there is little o work with' scores mark. Also allow any reasonable fon. Eg carbon may have been removed by bonding to ding material	
		Don't all	ow, ' <u>All</u> the carbon has decayed' 2	
			2	[6]
12	(a)	(i) 1/12 the mass	of an (atom) of $\frac{12}{8}$ C / carbon-12 / C12 $\checkmark$	
	(4)		nce to a nucleus loses the mark	
			1	
			leons have a greater mass 🗸 (than when inside a nucleus)	
		an answ	er starting with 'its' implies the nucleus	
		released wher	e (binding) energy <u>added</u> to <u>separate</u> the nucleons or energy is a nucleus is <u>formed</u> (owtte)	
			re independent of energy flow or work done must be explicit	
		uncetion	2	
	(b)	nuclei need to be <u>clo</u> fusion to take place	ose together (owtte) for the Strong Nuclear Force to be involved or for $\checkmark$	
		e.g. first	mark – within the range of the SNF	
		but the electrostatic	/ electromagnetic force is repulsive (and tries to prevent this) $\checkmark$	
		(if the temperature is the repulsion) 🗸	s high then) the nuclei have (high) kinetic energy / speed (to overcome	
		3 <sup>rd</sup> mark	is for a simple link between temperature and speed / KE 3	
	(c)	(i) 15 ✓		
		give the	middle mark easily for any e or $\beta$ with a + in any position	
		$e^+ \checkmark (or \beta^+, {0 \atop 1})$	β, <sup>0</sup> <sub>1</sub> e)	
		12 🗸		

 $\Delta$ mass = 4 × 1.00728 - 4.00150 - (2 × 9.11 × 10<sup>-31</sup> / 1.661 × 10<sup>-27</sup>) (ii) or ∆mass = {4 × 1.00728 - 4.00150 - 2 × 0.00055}(u) ✓ (4×1.00728=4.02912)  $1^{st}$  mark – correct subtractions in any consistent unit. use of  $m_p =$  $1.67 \times 10^{-27}$  kg will gain this mark but will not gain the 2<sup>nd</sup> as it will not produce an accurate enough result ∆mass = 0.02652(u) 🗸 2<sup>nd</sup> mark - for calculated value 0.02652u  $4.405 \times 10^{-29}$  kg  $3.364 \times 10^{-12} J$  $\Delta$ binding energy (= 0.02652 × 931.5) {allow 931.3}  $\Delta$ binding energy = 24.7 MeV  $\checkmark$ 3<sup>rd</sup> mark – conversion to Mev conversion mark stands alone award 3 marks for answer provided some working shown - no working gets 2 marks (2sf expected) 3 [12] insert control rods (further) into the nuclear core / reactor (a) a change must be implied for 2 marks marks by use of (further) or (more) allow answers that discuss shut down as well as power reduction which will absorb (more) neutrons (reducing further fission reactions) If a statement is made that is wrong but not asked for limit the score to 1 mark (e.g. wrong reference to moderator) 2 (b) fission fragments / daughter products or spent / used fuel / uranium rods (allow) plutonium (produced from U-238) 🗸 not uranium on its own 1 (c) (i) / (electromagnetic radiation is emitted) A reference to  $\alpha$  or  $\beta$  loses this first mark as the energy gaps are large (in a nucleus) as the nucleus de-excites down discrete energy levels to allow the nucleus to get to the ground level / state 🗸 mark for reason

2<sup>nd</sup> mark must imply energy levels or states

		(ii)	momentum / <u>kinetic energy</u> is transferred (to the moderator atoms) or a neutron slows down / loses <u>kinetic energy</u> (with each collision) 🗸		
			(eventually) reaching speeds associated with thermal random motion or reaches speeds which can cause fission (owtte) $\checkmark$		
				2	[7]
14	(a)	Draw	vs appropriate triangle on graph or other mark on graph at ~ 118		
			B1		
		Cha	nge of approx 1 Me V per nucleon is multiplied by 235		
			B1		
		Mult	iplies by 1.6 × $10^{-13}$		
			B1		
		Quo	tes their answer of approx 3.8 $\times$ 10 <sup>-11</sup> to more than 2 sf		
			B1		
				4	
	(b)	(2 × )	2.0135) – 4.0026 seen or 0.0244 (u)		
			C1		
		Mult	iplies u by $1.7 \times 10^{-27}$		
			C1		
		E=	$mc^2$ seen or multiplies by $(3 \times 10^8)^2$		
			C1		
		3 67	′ × 10 <sup>−12</sup> J		
		5.07			
			A1	4	

- M1 Compares  $5.5 \times 10^{14}$  (J) (Hydrogen) with  $9.6 \times 10^{13}$  (J) (Uranium) in some way eg by stating that the fusion reaction gives more energy (per kg) than the fission or very similar values - must be consequent on some correct analysis A1 Availability of fuel easier for fusion **B1** Doesn't produce radioactive fission products / no waste management problem **B1** (a)  $\binom{206}{76} X \rightarrow \frac{206}{82} Pb + \beta \times \frac{0}{-1} \beta + \beta \times \overline{v_e}$  $\beta = 6 \sqrt{}$ the energy **required** to split up the nucleus  $\checkmark$ (b) (i) into its individual neutrons and protons/nucleons  $\checkmark$ (or the energy **released** to form/hold the nucleus  $\checkmark$ from its individual neutrons and protons/nucleons  $\checkmark$ ) 7.88 × 206 = 1620 MeV √ (allow 1600-1640 MeV) (ii) U, a graph starting at  $3 \times 10^{22}$  showing exponential fall passing through (c) (i)  $0.75 \times 10^{22}$  near 9 × 10<sup>9</sup> years  $\checkmark$ Pb, inverted graph of the above so that the graphs cross at  $1.5 \times 10^{22}$  near  $4.5 \times 10^9$  years  $\checkmark$
- 2

attempts to convert to energy per kg by multiplying by 1000 / 4 or 1000 / 235

(d)

15

[13]

3

2

1

2

1

M1

(ii) (*u* represents the number of uranium atoms then)

$$\frac{u}{3 \times 10^{22} - u} = 2$$
$$u = 6 \times 10^{22} - 2u \checkmark$$
$$u = 2 \times 10^{22} \text{ atoms}$$

(iii) (use of 
$$N = N_0 e^{-\lambda t}$$
)

 $2 \times 10^{22} = 3 \times 10^{22} \times e^{-\lambda t} \checkmark$   $t = \ln 1.5 / \lambda$ (use of  $\lambda = \ln 2 / t_{1/2}$ )  $\lambda = \ln 2 / 4.5 \times 10^{9} = 1.54 \times 10^{-10} \checkmark$  $t = 2.6 \times 10^{9} \text{ years } \checkmark \text{ (or } 2.7 \times 10^{9} \text{ years)}$ 

3

1

[10]

1

## (a) any 2 from:

16

the sun, cosmic rays, radon (in atmosphere), nuclear fallout (from previous weapon testing), any radioactive leak (may be given by name of incident) nuclear waste, carbon-14  $\checkmark$ 

(b) (i) (ratio of area of detector to surface area of sphere)

ratio = 
$$\frac{0.0015}{4\pi (0.18)^2} \checkmark$$

(ii) activity =  $0.62/(0.00368 \times 1/400)$  give first mark if either factor is used.

67000  $\checkmark$  Bq accept s<sup>-1</sup> or decay/photons/disintegrations s<sup>-1</sup> but not counts s<sup>-1</sup>  $\checkmark$  (67400 Bq)

3

(c) (use of the inverse square law)

(a)

17

$$\begin{aligned} \frac{I_{1}}{I_{2}} &= \left(\frac{r_{2}}{r_{1}}\right)^{2} \text{ or calculating k} = 0.020 \text{ from I} = k/x^{2} \checkmark \\ I_{2} &= 0.62 \times \left(\frac{0.18}{0.28}\right)^{2} \checkmark 0.26 \text{ counts s}^{-1} \checkmark (\text{allow } 0.24 \text{-} 0.26) \end{aligned}$$

$$(i) \quad \text{Attempt to use KE} = 3/2 kT \text{ expect } 0.75 = 3/2 \times 1.38 \times 10^{-23} T \\ & \text{C1} \end{aligned}$$

$$(i) \quad \text{Attempt to use KE} = 3/2 kT \text{ expect } 0.75 = 3/2 \times 1.38 \times 10^{-23} T \\ & \text{C1} \end{aligned}$$

$$(i) \quad \text{Or correct conversion to J } 0.75 \times 1.6 \times 10^{-19} \\ \text{Correct equations } 0.75 \times 1.6 \times 10^{-19} = 3/2 1.38 \times 10^{-23} T \\ & \text{C1} \end{aligned}$$

$$(ii) \quad \text{Attempt to use energy} = qQ/4\pi\varepsilon_{o}r \\ & \text{C1} \\ \text{arrives at } 1.9(2) \times 10^{-9} \text{ or uses } (2 \times 0.75) \text{ or twice candidate's energy from (i)} \\ & \text{C1} \\ 9.6 \times 10^{-10} \text{ m} \\ & \text{A1} \\ & \text{A2} \\ & \text{A1} \\ & \text{A2} \\ & \text{A1} \\ & \text{A2} \\ & \text{A1} \\ & \text{A1} \\ & \text{A1} \\ & \text{A2} \\ & \text{A2} \\ & \text{A1} \\ & \text{A1} \\ & \text{A2} \\ & \text{A2} \\ & \text{A2} \\ & \text{A1} \\ & \text{A2} \\ & \text{A2} \\ & \text{A1} \\ & \text{A2} \\ & \text{A2} \\ & \text{A2} \\ & \text{A3} \\ & \text{A3} \\ & \text{A3} \\$$

[9]

	(iii)	For fusion nuclei have to touch or separation has to be nuclear diameter		
		energy has to be sufficient to overcome the nuclear repulsion (between protons)		
			B1	
		Close enough for nuclear strong force to act		
			B1	
		answer to 4 a (ii) is much greater that $10^{-15}$ m		
			B1	
		or is greater that atomic radius		
		or is greater than the range of the strong force		3
(b)	(i)	Use of <i>pV=NkT</i>		
			C1	
		(Allow incorrect powers of 10 or rearrangement to make <i>N</i> subject)		
		$1 \times 10^{16} \times 1 = N \times 1.38 \times 10^{-23} \times 1.5 \times 10^{6}$		
			C1	
		4.8 (3)× 10 <sup>32</sup>		
			A1	2
	(ii)	1.67 × 10 <sup>−27</sup> or 1.7 × 10 <sup>−27</sup> used		3
	(11)		C1	
			CT	
		8.0 – 8.2 × 10 <sup>5</sup> (kg m <sup>-3</sup> ) Allow ecf for <i>N</i> from (b)(i)		
			A1	2

(c)	(i)	Number of protons = moles of proton/mass of protons / Mass per second × Avogadro constant used			
			B1		
		Or			
		No of protons = mass per second/proton mass			
		(allow if numerical equation seen with a subject)			
		4.18 or 4.19 or 4.21 × $10^{38}$ correct to at least 2 sf from correct working			
			B1	2	
	(ii)	Attempt to use $E = mc^2$ with any mass and substitution for c		2	
	()	······	C1		
		Energy radiated = $5 \times 10^9 \times c^2$ energy radiated 4.5 × $10^{26}$ J			
			A1		
		Number of helium nuclei formed = $1.05 \times 10^{38}$ (allow $1 \times 10^{39}$ )			
			B1		
		Approximate BE per nucleon from article = $4.28(4.5) \times 10^{-12} \text{ J}$			
			B1		
		(Which is consistent)		4	
					[20]
(a)	(i)	energy released when the separate nucleons combine to form the nucleus			
		<b>or</b> energy needed to separate the nucleus into individual nucleon owtte	S		
			B1	1	
				1	

	(ii)	BE in J = 8 × 1.1314027 × 10 <sup>-12</sup> (9.05122 × 10 <sup>-12</sup> )		
			C1	
		BE in eV = $5.6570135 \times 10^7$ eV or BE/nucleon = $7.07 \times 10^6$ MeV		
			C1	
		56.570135 (MeV) (condone 3 sf consistent with electron charge)		
			A1	3
(b)	(i)	change in BE = 0.0147120 (× 10 <sup>-12</sup> ) J		3
(0)	(1)	Change in BL = 0.0147120 (x 10 ) 3	C1	
		use of $E = mc^2$ with their energy 1.635 × 10 <sup>-31</sup> kg		
			A1	2
	(ii)	use of charge on alpha particles = $2 e$		-
			C1	
		attempt to substitute in PE = $\frac{qQ}{4\pi\epsilon_0 r}$		
			C1	
		2.4(2.39) × 10 <sup>−13</sup> J		
			A1	

				B1		
			explains that when they touch there is zero KE only mass available is that of the two alpha particles			
				B1		
			extra KE provides the increase in mass of the beryllium-8 compared with the 2 He nuclei			
				B1	3	
						[12]
19	(a)	(i)	neutron			
19				B1		
		(::)			1	
		(ii)	p = 36	B1		
			n = 144			
				B1		
					2	
	(b)	(i)	total energy produced = $\frac{500 \times 100}{40}$ MJ each second			
				C1		
			number of reaction = $4.2 \times 10^{19}$ per second			
				A1	2	
					-	

	(ii)	1 kg contains (1000/235) × 6.02 × $10^{23}$ atoms of uranium	
			C1
		total number of fissions = $(1000/235) \times 6.02 \times 10^{23} \times 2 \times 10^4$ (5.1 × 10 <sup>28</sup> )	
			C1
		time = total fissions available/number per second or $1.2 \times 10^9$ s	
			C1
		38.7(39) years	
			A1
	(iii)	too few neutrons produced to maintain the chain reaction	
			B1
		probability of a neutron colliding with a uranium nucleus too low	
			B1
		more absorption of neutrons in non-fission capture	
			B1
(c)	pres	sure = $150 \times 10^5$ (Pa) or <i>F</i> = <i>PA</i>	
			C1
	force	e on 1 cm <sup>2</sup> = 1500N	
			A1

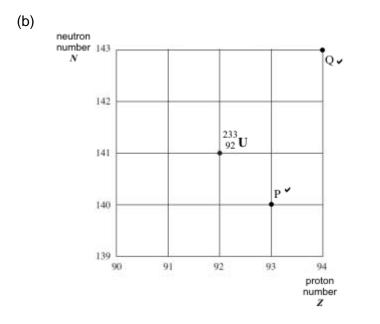
2

(d) energy removed each second

20

$$E = \frac{500 \times 100}{40}$$
 MJ = 1.25 × 109 J or  $E = mc\Delta\theta$ 

			C1		
		$1.25 \times 10^9 = m5000 \times 40$			
			C1		
		mass per second = 6250 kg			
			C1		
		volume per second = $8.6(8.56)$ m <sup>3</sup>			
			A1	4	
	(e)	control rods			
		neutrons are absorbed			
			B1		
		by the nucleus of the boron/atoms			
			B1		
		moderator neutrons are slowed down			
			B1		
		when colliding with the protons/hydrogen nucleus			
			B1		
				4	[21]
]		221			
	(a)	<sup>231</sup> 91 <b>Pa √</b>			
		anti (electron) neutrino 🗸		2	



(c) (i) 
$$x = 4 \sqrt{2}$$

(ii) mass defect = [(232.98915 + 1.00867) - (90.90368 + 138.87810 + 4 × 1.00867)] u √

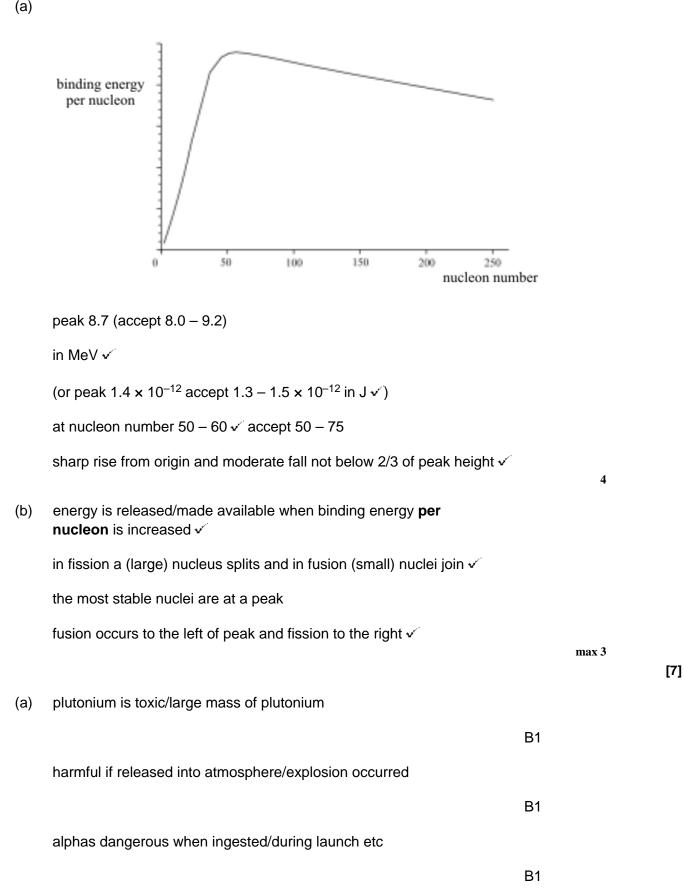
= 0.18136 u 🗸

energy released (= 0.18136 × 931) = 169 (MeV) √

[8]

2

1



22

max2

		nical bonding involves electrons (atomic) pactivity is nuclear (owtte)/same number of nuclei ent		
			B1	2
(c)	(i)	$T_{\gamma_2} = \ln 2/\lambda$		
			C1	
		$2.51 \times 10^{-10}$		
			A1	2
	(ii)	molar mass calculated (0.270 kg)	0.4	
		use of 33 kg	C1	
			C1	
		number of moles in sample (122.2)		
			C1	
		multiplication of value by Avogadro's number	01	
		7.36 × 10 <sup>25</sup>	C1	
			A1	
	(iii)	(c) (i) × (c) (ii)		5
	ζ, γ		C1	
		1.83 × 10 <sup>16</sup> cao		
			A1	
		Bq	5.4	
			B1	3

B1

			B1		
		alpha correct (4,2) – accept He or $\alpha$ symbol			
			B1	2	
		(ii) use of 1 g generating 500 mW			
			C1		
		16500 W total			
			C1		
		recognition that activity × energy of one alpha = power	C1		
		9.00 × 10 <sup>−13</sup> (J)	01		
			A1		
				4	[20]
23	(a)	correct numbers for beta+ $(0, (+)1)$ and chromium (52)			
			B1		
		(electron) neutrino with correct numbers (0,0)			
			B1	2	
	(b)	W <sup>+</sup> /W/(intermediate vector) boson (not Z boson)			
			B1	1	
					[3]
24	(a)	probability of decay per unit time/given time period			
		or fraction of atoms decaying per second			
		or the rate of radioactive decay is proportional to the number of (unstab nuclei	le)		
		and nuclear decay constant is the constant of proportionality (1)		1	

(b) use of 
$$\frac{T_1}{2} = \frac{ln2}{\lambda}$$

$$T_{\frac{1}{2}} = \ln 2/3.84 \times 10^{-12} \text{ s} (1) (1.805 \times 10^{11} \text{ s})$$
$$= (1.805 \times 10^{11}/3.15 \times 10^{7}) = 5730 \text{ y} (1)$$
answer given to 3 sf (1)

(c) number of nuclei =  $N = 3.00 \times 10^{23} \times 1/10^{12}$  (1)

(using 
$$\frac{\Delta N}{\Delta t} = -\lambda N$$
)

rate of decay =  $3.84 \times 10^{-12} \times 3.00 \times 10^{11}$  (1)

(d)  $(N = N_0 e^{-\lambda t})$  and activity is proportional to the number of nuclei  $A \mu N$  use of  $A = A_0 e^{-\lambda t}$ 

$$0.65 = 1.15 \times e^{-3.84 \times 10^{-12}t}$$
(1)

$$t = \frac{\ln\left(\frac{1.15}{0.65}\right)}{3.84 \times 10^{-12}} \text{ or } \frac{\ln\left(\frac{0.651}{1.15}\right)}{-3.84 \times 10^{-12}}$$

3

3

2

(e) the boat may have been made with the wood some time after the tree was cut down

the background activity is high compared to the observed count rates

the count rates are low or sample size/mass is small or there is statistical variation in the recorded results

possible contamination

uncertainty in the ratio of carbon-14 in carbon thousands of years ago any two (1)(1)

25	(a)	number correct for alpha (1)	
		number correct for beta (1)	
		alpha decay first goes via TI <b>(1)</b>	
		numbers correct for TI (208, 81) (1)	
		beta decay first goes via Po (1)	
		numbers correct for Po (212, 84) (1)	6
	(b)	<ul> <li>(i) use of GM tube + counter/rate-meter (1) measurement of count rate (1) at range of distances + suitable ruler or tape measure (1) specifies suitable range (1) determines background &amp; corrects (1) safety precaution given (1) graph of count rate or corrected count rate against 1/d<sup>2</sup> (1)</li> </ul>	max 6
		<ul> <li>(ii) gamma not absorbed (1) spreads uniformly from a point source/spherically symmetrically (1) area over which it spreads is proportional to radius squared (1) alpha and beta are absorbed in addition to spreading out (1)</li> </ul>	max 3
26	(a)	for one reaction $\Delta E (= \Delta m c^2) = 3.1 \times 10^{-28} \times (3.00 \times 10^8)^2$ (1) = (2.79 × 10 <sup>-11</sup> J) number of nuclei required = $\frac{1}{2.79 \times 10^{-11}} = 3.5(8) \times 10^{10}$ (1)	
		[or equivalent credit for any other valid method]	2

[15]

(b) output power from reactor =  $\frac{600}{0.35} = 1700$  (MW) (1)

(1714 MW)

energy output from fuel rods in one week =  $1.70 \times 10^9 \times 24 \times 7 \times 3600$  (1)

$$\Delta m \left( = \frac{\Delta E}{c^2} \right) = \frac{1.03 \times 10^{15}}{(3.0 \times 10^8)^2}$$
 (1)

= 1.14 ×10<sup>-2</sup> kg (1)

[or equivalent credit for any other valid method]

(a)

$$R (= r_0 A^{1/3}) = 1.3 \times 10^{-5} \times (238)^{1/3} (1)$$
  
= 8.0(6) × 10<sup>-15</sup>m (1)

(b) (use of inverse square law e.g. 
$$\frac{I_1}{I_2} = \left(\frac{x_1}{x_2}\right)^2$$
 gives)

$$10 = \left(\frac{x_2}{0.03}\right)^2 (1)$$

*x* = 0.095 m **(1)** (0.0949 m)

(c) (use of  $A = A_0 exp(-\lambda t \text{ gives}) 0.85 = 1.0 exp(-\lambda 52)$  (1)

$$\hat{\lambda} = \frac{\ln(100/0.85)}{52}$$
(1)  
= 3.1(3) × 10<sup>-3</sup>s<sup>-1</sup> (1)

(d) it only emits  $\gamma$  rays (1)

relevant properties of  $\gamma$  radiation e.g. may be detected outside the body/weak ioniser and causes little damage (1) it has a short enough half-life and will not remain active in the body after use (1) it has a long enough half-life to remain active during diagnosis (1) the substance has a toxicity that can be tolerated by the body (1) it may be prepared on site (1)

any three (1)(1)(1)

3

4

2

2

3

[6]

(a)

(i) heat water to 100 °C, energy (= 190 × 4200 × 79) = 63 (MJ) (1) vapourise water, energy
 (=190 × 2.3 × 10<sup>6</sup>) = 440(MJ) (1) (437MJ)

energy transferred (per sec) = (437 + 63) MJ (1) (= 500 MJ)

(ii) mass of rocks (=  $4.0 \times 10^6 \times 3200$ )

= 
$$1.3 \times 10^{10}$$
(kg) (1)  
(1.28 ×  $10^{10}$ )

temperature fall of  $\Delta T$  in one day, energy removed (= 1.28 ×10<sup>10</sup> × 850 ×  $\Delta T$ ) = 1.1 × 10<sup>13</sup>  $\Delta T$  (1) (1.09 × 10<sup>13</sup> AT) (allow C.E. for value of mass of rocks)

energy transfer in one day (=  $500 \times 10^6 \times 3600 \times 24$ ) =  $4.3 \times 10^{13}$  (J) (1)

in one day 
$$\Delta T \left( = \frac{4.3 \times 10^{13}}{1.1 \times 10^{13}} \right) = 3.9(1)$$
 K (1)

(b)	number of nuclei in 1 kg of <sup>238</sup> U	=	$\left(\frac{6.02 \times 10^{23}}{0.238}\right)$	$= 2.5(3) \times 10^{24}$	(1)
-----	--	---	--	---------------------------	-----

activity of lkg of <sup>238</sup>U =  $\frac{1n2}{T_{1/2}} \times 2.53 \times 10^{24}$  (1)

$$\left(=\frac{1n2}{4.5\times10^9\times3.1\times10^7}\times2.53\times10^{24}\right)=1.2(6)\times10^7(s^{-1})$$
 (1)

energy released per sec per kg of 238 U

= 
$$1.2(6) \times 10^7 \times 4.2 \times 1.6 \times 10^{-13}(J)$$
 (1)  
(8.47 × 10<sup>-6</sup>(J))

mass of <sup>238</sup>Uneeded = 
$$\frac{500 \times 10^6}{8.47 \times 10^{-6}}$$
 = 5.9(0) × 10<sup>13</sup>kg (1)

(a) graph passes through N = 10/11 when Z = 10 and N increases as Z increases (1) N = 115  $\rightarrow$  125 when Z = 80 and graph must bend upwards (1)

2

5

7

[12]

(b)	(i) <b>W</b> at $Z > 60$ just (within one diagonal of a square) below line (1)		
	(ii) <b>X</b> just (within one diagonal of a square) above line <b>(1)</b>		
	(iii) <b>Y</b> just (within one diagonal of a square) below line <b>(1)</b>	3	
(C)	working showing the change due to emission of four $\alpha$ particles (1) four $\beta^-$ particles (1)		
(പ)	Any two from the following list of processor	1	
(d)	Any <b>two</b> from the following list of processes:		
	$\beta^+$ describe the changes to <i>N</i> (up by 1) and <i>Z</i> (down by 1) [or allow p change to n]		
	α move closer to line of stability [or state the proton to neutron ratio is reduced]		
	p only if nuclide is <b>very</b> proton rich [or electrostatic repulsion has to overcome the strong nuclear force] [or highly unstable] [or rare process]		
	e <sup>-</sup> capture describe the changes to $N$ (up by 1) and $Z$ (down by 1) allow p changes to n		
	marking: listing <b>two</b> processes <b>(1)</b> discussing <b>each</b> of the two processes <b>(1) (1)</b>		
		QWC 1	[10]
(a)	reasons: $\alpha$ particle has much more mass/momentum than $\beta$ particle $\alpha$ particle has twice as much charge as a $\beta$ particle $\alpha$ particle travels much slower than a $\beta$ particle any <b>two (1) (1)</b>	2 QWC 1	
(b)	(i) energy absorbed per sec (= energy released per sec) = $3.2 \times 10^9 \times 5.2 \times 10^6 \times 1.6 \times 10^{-19}$ (1) = $2.7 \times 10^{-3}$ (J) (1) (2.66 × $10^{-3}$ (J))		

(ii) temperature rise in 1 minute  $\left(=\frac{\text{energy absorbed in 1 minute}}{\text{mass} \times \text{specific heat capacity}}\right)$ 

$$= \frac{2.7 \times 10^{-3} \times 60}{0.20 \times 10^{-3} \times 900}$$
 (for numerator) (1) (for denominator) (1)

= 0.90 K (or °C) (1)

(allow C.E. for incorrect value in (i))